

2^n grows fast

$\log_2 n$ shrinks fast

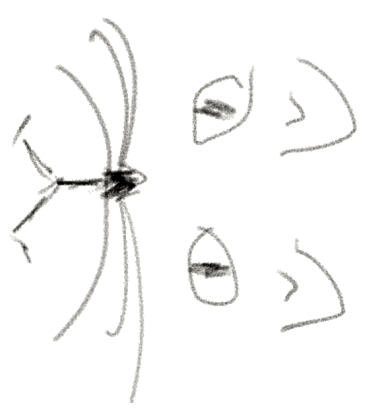
thank u



The POWER of Ω

A zine about big numbers & by Igor

hi D
 This is a
 ZINE
 about
 BIG
 NUMBERS



MEOW

$O(2^n)$

$O(\log n)$

and this scales D
 atoms in a human body:

7×10^{27}

$\log_2 \Rightarrow$

92

atoms in the observable

universe:

4×10^{79}

$\log_2 \Rightarrow$

264

even if you have

18 QUINTILLION

records, that will only
require **64** comparisons
to find a value.

$$\log_2(18'446'744'033'705'554'616) = 64$$

This means:

if you had 18 quintillion
addresses, you would only
have to try on 64 of them
to find the right size.

MY NAME IS IGOR

@igorwhilefalse

ON THE TWITTERWEB

i have a

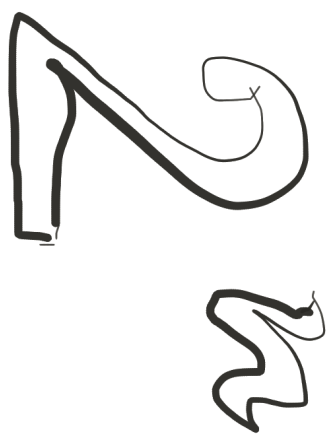
Sticker

Stickers on my phone

i got it from @bDrk!

FIRST, LET'S TALK

ABOUT EXPONENTIATION

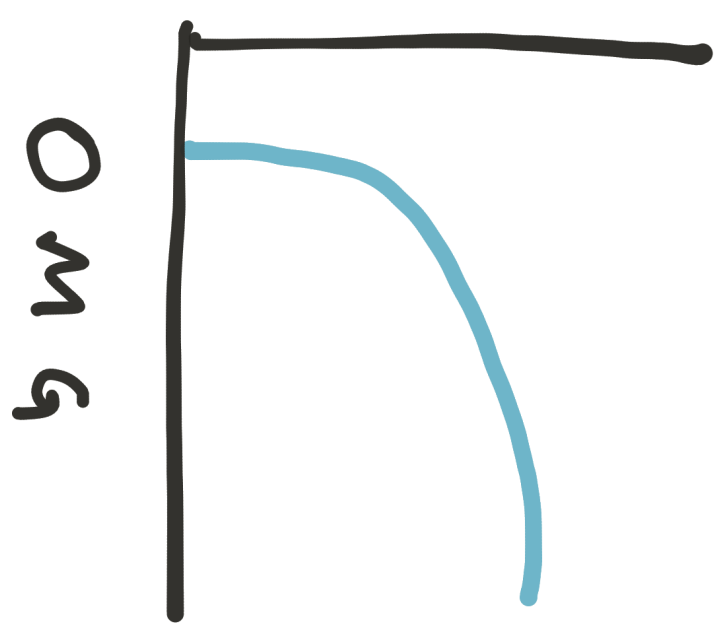


THAT MEANS:

$2 \times 2 \times 2 \times \dots$

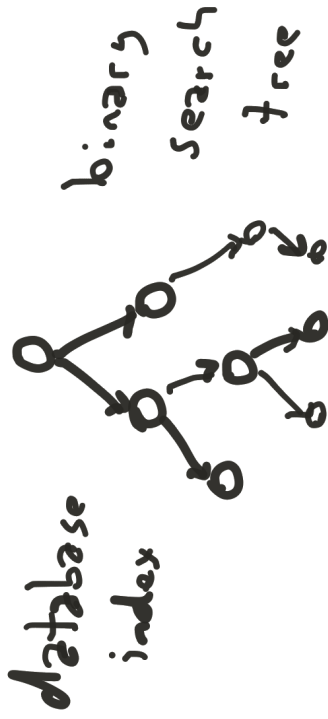


$\log_2 n$
Shrinks fast!



databases use binary search

they are literally the same thing as finding a fitting dress!



This is why data

bases work and are

FAST

THE STORY OF

SISSA BEN DAHIR

he goes to the Queen

and gives her a chess-board,

i have 1 grain of

RICE, for the first

square, give me 2 grains.

for the second, give

me 4. for the third

give me 8. 2x

she agrees, so they start bringing in the rice.

2	4	8	16	32	64	128	256
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after one row we have 256 grains.

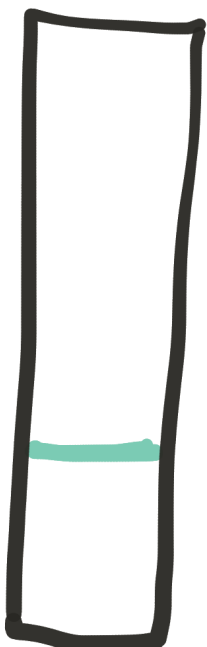
512	1024	2048	4096	8192	16384	32768	65536
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but after two rows we are already at 65K!

OH NO



you will quickly approach the size you are looking for!



this works because the dresses are sorted. the algorithm is called a

BINARY SEARCH

it will let you find a fitting dress in

LOGARITHMIC TIME

so you move to the middle of
 the upper half, take out a dress,
 try it on.



if it's too large, the dress must be
 somewhere in the lower half.



so you go to the middle..



WHAT HAPPENS IF WE KEEP GOING
 ?

2	4	8	16	32	64	128	256
512	1024	2048	4096	8192	16384	32768	65536

How much rice?

IF WE COMPLETE THE BOARD

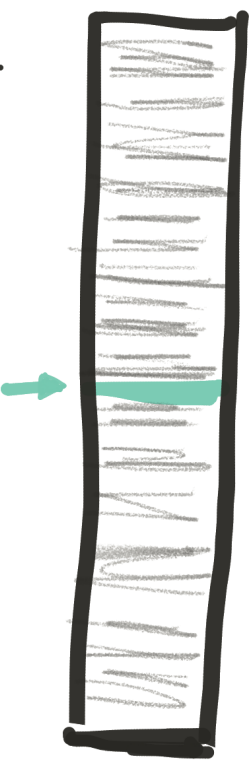
...

2	4	8	16	32	64	128	256
5 12	10 24	20 48	40 96	80 192	160 384	320 768	640 1536
13 1K	26 2K	52 4K	1M	2M	4M	8M	16M
33M	67M	134M	268M	536M	1B	2B	4B
8B	17B	34B	68B	137B	274B	548B	1T
2T	4T	8T	17T	35T	70T	140T	281T
562T	1Q	2Q	4Q	9Q	18Q	36Q	72Q
144Q	288Q	576Q	1 quint	2 quint	4 quint	9 quint	18 quint

WE END UP WITH

18 QUINTILLION

Here is an algorithm that lets you do that!



start in the middle. take out a dress, try it on. if it's too small, you know your dress is in the upper half.



let's say you go **DRESS SHOPPING**

and you see a super cute

dress WITH POCKETS!

YAY CHECK OUT
That dress!

it comes in 200 sizes.



you want to find
one that fits.

they're sorted by size

18'446'744'073'709'551'616

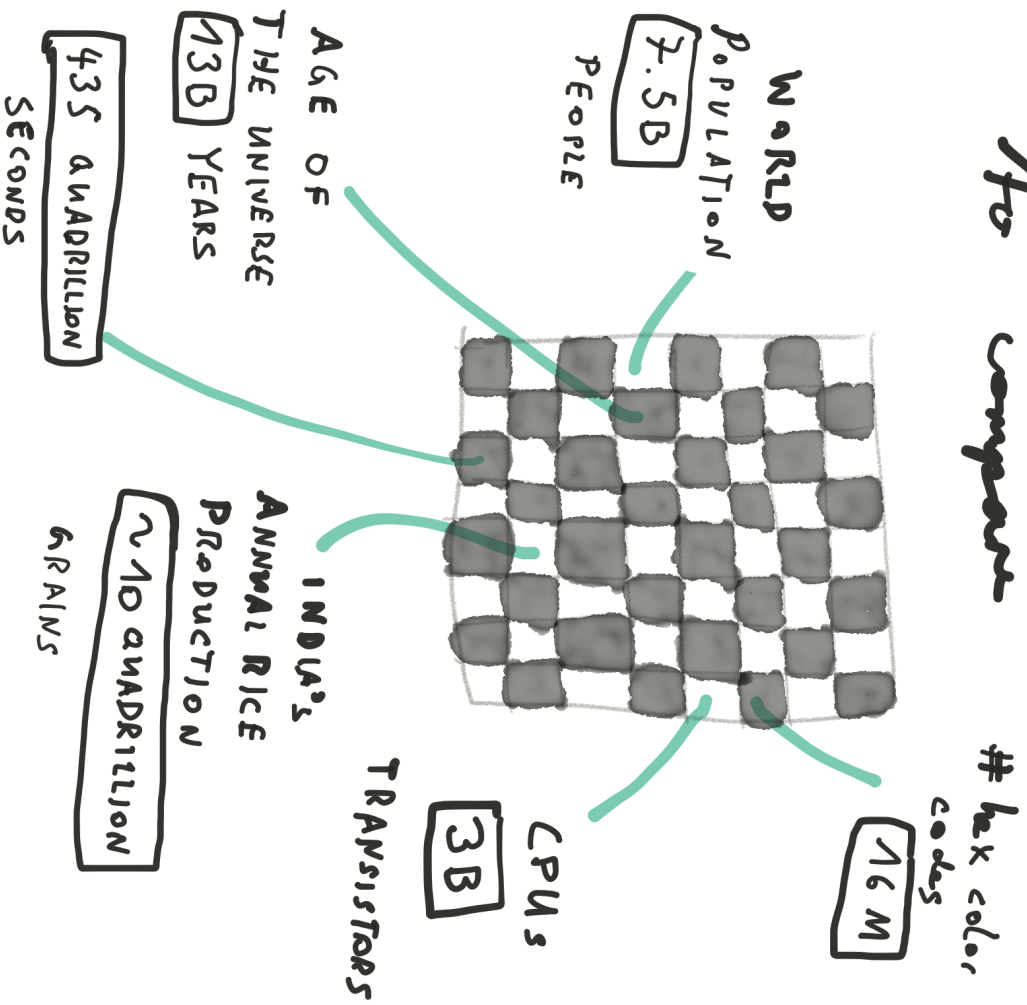
Grains of rice



of rice

BIG NUMBERS

For comparison



NEXT UP

The Logarithm

$$\log_2 n$$

$$n \div 2 \div 2 \dots = 1$$

$$\xrightarrow{y}$$

This is going to
Blow Your MIND!

JUST WANTED TO

LET YOU KNOW

COMPUTERS

ARE GREAT

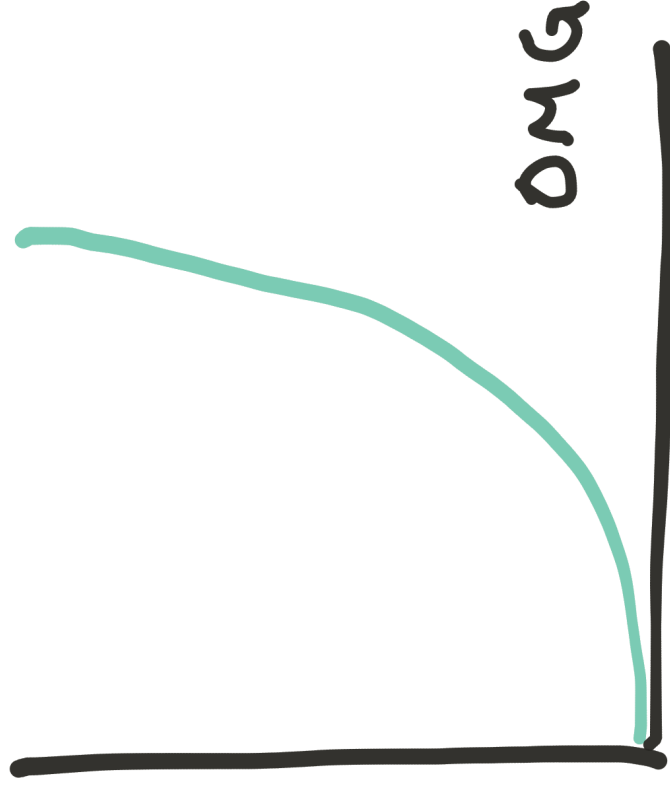
(I love them)

but don't forget
about HUMANS



2^n grows

fast



Other examples of

EXPONENTIAL GROWTH

- POPULATION
 - ZOMBIE INFECTION
 - ECONOMIC MODELS (LOL)
 - MOORE'S LAW
- COMPUTERS KEEP GETTING
≡ FASTER
(BUT NOT FOREVER)

Exponential growth makes

Your password safe \ominus

1 char = 16 possible values

2 chars = 256 possible values

16 chars = 18 QUINTILLION



Same for a 64-bit key

$$2^{64} = 18 \text{ QUINT.}$$



CRYPTO